TITLE OF THE INVENTION

HADAMARD TRANSFORMATION METHOD AND DEVICE

FIELD OF THE INVENTION

5   The present invention relates to an Hadamard

transformation method and device capable of making the

reversible transformation to output the integer data.

BACKGROUND OF THE INVENTION

10   An image, especially a multi-valued image contains

a very large amount of information, and when the image

is stored or transmitted, its data amount causes a

problem. Therefore, to store or transmit the image, a

high efficient coding is employed for coding the image

15   data, in which the multi-valued image has the

redundancy removed, or the content of the multi-valued

image is changed to the extent that the image quality

degradation is visually unrecognizable to reduce the

data amount. For example, in a JPEG recommended by the

20   ISO and ITU-T as the international standard coding

system for still image, the image data is subjected to

a Discrete Cosine Transformation (DCT) into DCT

coefficients for each block (8 pixels × 8 pixels), each

DCT coefficient being quantized, and further the

25   quantized value is entropy coded to compress the image

data. The compression techniques using this DCT

include H261, MPEG1/2/4, in addition to the JPEG.

An Hadamard transformation is a process associated with this DCT transformation or a process for transforming the image data. The Hadamard transformation is an orthogonal transformation with a

5   transformation matrix composed of the elements of "1" and "-1", which is the simplest one that is represented only by addition and subtraction.

For this Hadamard transformation, a transformation matrix H_2 for two-point Hadamard transformation is

10   defined in the following way.
[Expression 1]

$$H_2 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \qquad (1)$$

A typical N ($=2^N$)-point Hadamard transformation matrix H_N is recursively defined as a Kronecker product

15   between the (N/2)-point Hadamard transformation matrix $H_{N/2}$ and the two-point Hadamard transformation matrix H_2.
[Expression 2]

$$\begin{aligned} H_N &= H_{N/2} \otimes H_2 \\ &= \frac{1}{\sqrt{2}} \begin{bmatrix} H_{N/2} & H_{N/2} \\ H_{N/2} & -H_{N/2} \end{bmatrix} \end{aligned} \qquad (2)$$

A four-point Hadamard transformation matrix is

20   obtained from the above definition in the following way.
[Expression 3]

$$H_4 = \frac{1}{2}\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix} \qquad (3)$$

This four-point Hadamard transformation matrix is called a natural type, in which the base vectors are not arranged in sequency. Thus, if the permutation of the base vectors is repeated to shift the base vector in the second row to the fourth row, a transformation matrix WH_4 having the base vectors arranged in sequency results.

[Expression 4]

$$WH_4 = \frac{1}{2}\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix} \qquad (4)$$

This transformation matrix WH_4 is called a Walsh type or a Walsh-Hadamard transformation matrix. It is well known that the Hadamard transformation is a reversible orthogonal transformation, in which both the natural type and the Walsh type are capable of the reversible transformation, and the transformation matrix is symmetrical.

It is generally said that the Hadamard transformation is a reversible transformation as is described above, which means that it is mathematically reversible. That is, it is supposed that no

arithmetical operation error arises in the transformation and the reverse transformation. For this reversible transformation, it is required to perform the arithmetical operation in the fixed point

5   and the floating point, and hold all the data of significant digits after the transformation processing.

However, in the Hadamard transformation in which the compression coding is supposed, there is a desire to reduce the number of significant digits as much as

10   possible after the transformation processing. More specifically, the data after the decimal fractions that arises when the integer input data is transformed is grasped to have clearly more digits (information) than the input data, whereby it is indispensable to omit the

15   data after the decimal fractions to compress the data. However, if this data after the decimal fractions is simply rounded, the reversible property is impaired. For example, four pieces of data, including 123, 78, 84 and 56, are subjected to the Hadamard transformation

20   with a transformation matrix of the expression (4) in the following way.

170.5(=(123+78+84+56)/2), 30.5(=(123+78-84-56)/2), 8.5 (=(123-78-84+56)/29, 36.5(=(123-78+84-56)/2)

Rounding off the above values into the integer,

25   171, 31, 9, 37

are obtained. Then, making the reverse transformation
(with a transposed matrix of the transformation matrix,
which is the same as the transformation matrix),

   124, 78, 84, 56

are obtained. In this way, the initial data "123" is
altered into "124" through the Hadamard transformation
and its reverse transformation. Thus, the Hadamard
transformation to output the integer data does not
guarantee the reversibility. In the following, the
Hadamard transformation to output the integer data is
called an integer type Hadamard transformation, and the
integer type Hadamard transformation capable of making
the reversible transformation is called an integer type
reversible Hadamard transformation or a lossless
Hadamard transformation.

   Conventionally, the lossless four-point Hadamard
transformation was realized in the following way.

(a) Decompose the four-point Hadamard transformation
matrix H_4 into a product of triangular matrices with
the diagonal elements "1",

(b) Apply a row replacing operation Q on the original
transformation matrix, and

(c) Decompose QH_4 into a product of following matrices
from the above (a) and (b).

[Expression 5]

$$QH_4 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & -1 & 1 & 0 \\ -1 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1/2 & 1/2 \\ 0 & 1 & 1/2 & -1/2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{bmatrix} \qquad (5)$$

(d)   Represent this transformation in a signal flow (as represented in FIG. 1),

(e)   Round the data after the decimal fractions that arises in multiplication operation in this signal flow to make the integer data.

The lossless four-point Hadamard transformation is implemented with the above items (a) to (e). Some supplementary explanation is given in the following.

The signal flow of FIG. 1 has a Ladder Network configuration which is often employed to implement a reversible transformation process. In this Ladder Network, the transformation process for outputting the integer data is made reversible by introducing a rounding process (200, 201 in FIG. 2) rounding the data to the output side of a multiplier 100, 101 in which the data after the decimal fractions is produced as a general method (in the field of reversible transformation process).

Herein, if the corresponding rounding process of the multiplication output is the same between the transformation process and the reverse transformation process, the content of the rounding process 200, 201 is arbitrary.

FIG. 2 shows a signal flow (capable of the reversible transformation) which is made reversible by introducing the rounding process into the signal flow of FIG. 1. This was a conventional arithmetical operation method for implementing the integer type reversible four-point Hadamard transformation.

A lossless 16-point Hadamard transformation is constructed by linking such lossless integer type reversible four-point Hadamard transformations at multistage. However, there is a dispersion in the average value of the error of each transformed output (a difference between mathematical transformation and lossless transformation) or the mean square error, giving rise to accurate transform coefficients and inaccurate transform coefficients .

Also, the conventional lossless two-dimensional DCT (Discrete Cosine Transformation) had a significant error of transformation with reference to the conventional two-dimensional DCT.

SUMMARY OF THE INVENTION

The present invention has been achieved in the light of the above-mentioned conventional example, and the feature of the invention is to provide an Hadamard transformation method and device in which the content of rounding process is set up so that the mean error occurring in the lossless Hadamard transformation

process is theoretically zero to enhance the precision of transform coefficients .

According to the present invention, there is provided an Hadamard transformation method comprising:

5   a first transformation step of transforming input signals using a four-point Hadamard transformation matrix in each of four four-point Hadamard transformation units; a first rounding step of rounding up the least significant bit of each of the odd number

10   of four coefficients transformed by each of the four four-point Hadamard transformation units and discarding the least significant bit of each of the remaining odd number of the four coefficients, so as to produce the integer type of four sets of coefficients, each set

15   including four coefficients; a second transformation step of selecting one coefficient from each one set of the four sets such that odd numbers of coefficients among the four selected coefficients for one set were rounded up in the first rounding step, and supplying

20   the four selected coefficients to a four-point Hadamard transformation unit and transforming the four selected coefficients using a four-point Hadamard transformation matrix; and a second rounding step of rounding up the coefficients transformed in the second transformation

25   step so as to cancel propagation errors to be superposed over the transformed coefficients.

Other features and advantages of the present invention will be apparent from the following description taken in conjunction with the accompanying drawings, in which like reference characters designate 5 the same or similar parts throughout the figures thereof.

BRIEF DESCRIPTION OF THE DRAWINGS

The accompanying drawings, which are incorporated 10 in and constitute a part of the specification, illustrate embodiments of the invention and, together with the description, serve to explain the principles of the invention.

FIG. 1 depicts a diagram showing a signal flow 15 that is a basis for implementing a conventional lossless 4×4 Hadamard transformation process;

FIG. 2 depicts a diagram showing a signal flow of the conventional lossless 4×4 Hadamard transformation process;

20 FIG. 3 depicts a block diagram showing the configuration of a lossless 16-point Hadamard transformation using lossless 4×4 Hadamard transformations;

FIGS. 4A to 4H depict diagrams showing eight types 25 of lossless four-point Hadamard transformation as already proposed by the present inventor;

FIG. 5 depicts a block diagram showing the configuration of a lossless 16-point Hadamard transformation according to a first embodiment of the invention;

5   FIGS. 6A to 6C are graphs showing a transformation error distribution in the lossless 16-point Hadamard transformation process according to the first embodiment of the invention;

FIG. 7 depicts a diagram showing one example of

10   the configuration in which the mean error in transformation is not zero in contrast to the lossless 16-point Hadamard transformation of FIG. 5 according to the first embodiment of the invention;

FIGS. 8A to 8C are graphs showing the

15   transformation error distribution in the configuration of FIG. 7;

FIG. 9 depicts a block diagram showing the configuration of a lossless two-dimensional Hadamard transformation according to a second embodiment of the

20   invention;

FIG. 10 depicts a diagram showing the configuration of a lossless DCT as described in document 2;

FIG. 11 depicts a block diagram showing the

25   configuration of a conventional lossless two-dimensional DCT;

FIG. 12 depicts a block diagram showing the configuration of a lossless two-dimensional DCT according to a third embodiment of the invention;

FIG. 13 depicts a diagram showing the configuration of a one-dimensional DCT that is effective for the lossless two-dimensional DCT according to the third embodiment of the invention; and

FIG. 14 depicts a table showing the comparison of the reverse transformation precision of the lossless two-dimensional DCT.

DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

The preferred embodiments of the present invention will be described below with reference to the accompanying drawings.

[First Embodiment]

FIG. 3 is a block diagram showing the configuration of the lossless 16-point Hadamard transformation using lossless 4×4 Hadamard transformations.

As shown in FIG. 3, the eight lossless four-point Hadamard transform sections 300 to 307 are linked at multistage. Herein, 16 pieces of input data (d0 to d15) are divided into four blocks, and each block is subjected to the lossless four-point Hadamard transformation by each of the lossless four-point Hadamard transform sections 300 to 303. Then, four

transform coefficients at the same level in each
transformation by the lossless four-point Hadamard
transform sections 300 to 303 are gathered, and the
four transform coefficients are subjected to the

5   lossless four-point Hadamard transformation again by
the lossless four-point Hadamard transform sections 304
to 307, respectively, to implement the lossless 16-
point Hadamard transformation.

Herein, the lossless four-point Hadamard transform

10   sections 300 to 307 may employ the Hadamard
transformation configuration as shown in FIG. 2, or may
employ lossless Hadamard transformations with any one
of eight types of rounding process described later.

Explaining simply, the eight types of the rounding

15   process comprise rounding up the odd number of four
transform coefficients and rounding down the remaining
odd number of the four transform coefficients. In
other words, one or three the four transform
coefficients are rounded up and the remaining

20   coefficients are rounded down.

FIGS. 4A to 4H depict diagrams showing the
processings in eight types of lossless four-point
Hadamard transform sections. Herein, the
transformation process with the Hadamard transformation

25   matrix according to the expression (3) or (4) is
performed by each of the four-point Hadamard transform
sections 410 to 417 at the former stage, and the

rounding process is performed by 400 to 407 at the latter stage. Herein, the content of the rounding process is simply indicated as "+" and "-", in which "+" means the round-up and "-" means the round-down

5 (discard). The round-up and round-down as used in this specification means the rounding up and discarding process on two's complement representation, but not the absolute value representation. For example, a complement representation of "-7.5" is "11111000.1", in

10 which if this fraction part is rounded up, "11111001" (-7) results, and if it is rounded down, "11111000" (-8) results.

The reverse transformation is also one kind of lossless transformation. Its reason is that if the

15 data after reverse transformation is transformed again, the data becomes equal to the data before the reverse transformation. Hence, the eight types of lossless four-point Hadamard transform sections 410 to 417, 400 to 407 as shown in FIGS. 4A to 4H shows also all types

20 of reverse transformation. The correspondence between transformation and reverse transformation is different depending on the type of Hadamard transformation matrix (natural type or Walsh type).

The natural type has the following relationship

25 between the transformation and the reverse transformation as indicated by drawing numbers.

    (4A) → (4A);

(4B) → (4G);

(4C) → (4F);

(4D) → (4H);

(4E) → (4E);

5   (4F) → (4C);

(4G) → (4B);

(4H) → (4D)

Also, the Walsh type has the following
relationship between the transformation and the reverse
10 transformation as indicated by drawing numbers.

(4A) → (4A);

(4B) → (4F);

(4C) → (4H);

(4D) → (4G);

15 (4E) → (4E);

(4F) → (4B);

(4G) → (4D);

(4H) → (4C)

In natural type or Walsh type, the rounding
20 process is adapted to cancel a propagation error in the
reversed transformed data.

In the following description, the transformation
matrix of Walsh type is employed, unless specifically
noted.

25 The lossless 4×4 Hadamard transformation using any
of the eight types of the rounding process as shown in
FIGS. 4A to 4H may be equally applied in FIG. 3 to make

the lossless 16-point Hadamard transformation. There
are 8^8 kinds of combinations. Thus, the following
issues are imposed.

(A1) Make the mean error for each transform coefficient
zero.

The random number without correlation is assumed
as the input data. The lossless 16-point Hadamard
transformation satisfying the issue (A1) is configured
on the basis of the following conditions (B1) and (B2).

(B1) For the four intermediate data input into each of
the Hadamard transform sections 304 to 307 at the
second stage (latter stage), the rounding process at
the first stage is decided such that the odd number of
data are rounded up, and the remaining odd number of
data are rounded down. Then, the rounding process at
the first stage is of course one of the eight types of
rounding process.

(B2) Each of the Hadamard transform sections 304 to 307
at the second stage decides the type of rounding
process to make the reverse transformation, grasping
four input data as being generated from the same
Hadamard transformation.

Of the four Hadamard transform sections 300 to 303
at the first stage, up to three Hadamard transform
sections can freely decide the rounding process, but
the remaining one has the rounding process uniquely
decided if the condition (B1) is satisfied. Further,

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the four Hadamard transform sections 304 to 307 at the
second stage uniquely decided if the condition (B2) is
satisfied. In this way, the configuration to satisfy
the conditions (B1) and (B2) is simply obtained, and
5   has the 512 (= 8^3) types.

FIG. 5 depicts a block diagram showing the
configuration of the lossless 16-point Hadamard
transformation according to the first embodiment of the
invention. The four-point Hadamard transform sections
10   501 to 504 and 521 to 524 in FIG. 5 have the same
configuration as the four-point Hadamard transform
sections 410 to 417 as shown in FIGS. 4A to 4H.

In FIG. 5, "+" in the rounding processes 511 to
514 and 531 to 534 denotes the round up, and "-
15   " denotes the discard. In this example, seven types of
rounding operation are employed among all the eight
types of operations. When configured in this way, the
mean error of arbitrary output becomes not only "0",
but also the error distribution is the same, whereby
20   the mean square error becomes equal. In the following,
the reason why the mean error becomes "0" through the
error distribution will be described.

In FIG. 5, four inputs (intermediate data) for
each of the Hadamard transform sections 521 to 524 at
25   the second stage have no correlation because they are
not supplied from the same Hadamard transform section.
For example, a superposed error in the input data into

the Hadamard transform section 521 occurs at the same
probability in all sixteen cases from (0, 0, 0, 0) to
(+0.5, -0.5, -0.5, -0.5). In FIG. 5, the intermediate
data 540 is the rounded up data of a transformed

5   coefficient and contains a round-up error (+0.5) at a
probability of 1/2, and the transformed coefficient is
the integer and error free data at a probability of 1/2.
For other three intermediate data 541 to 543, the
rounding process is the discard, in which an error (-

10   0.5) due to the discard occurs at a probability of 1/2
in each intermediate data, and each transformed
coefficient is the integer and error free data at a
probability of 1/2 in the same way as above.

The values which are the product of 1/2 and the

15   inner product between this superposed error and the
first row of the transformation matrix in the
expression (4), are distributed from the minimum "-
0.75" to the maximum "0.25" at a step of "0.25". More
particularly, the values of "-0.75", "-0.5", "-0.25",

20   "0", and "+0.25" are distributed at the probabilities
of "1/16", "1/4", "3/8", "1/4" and "1/16", respectively.
FIG. 6A shows this distribution. If this distribution
has "+0.5" added in a rounding process 531 after
transformation process by the Hadamard transform

25   section 521 at the second stage, the error distribution
is as shown in FIG. 6B.

In this case, the probability that "+0.5" is added in the rounding process 531 after transformation process by the Hadamard transform section 521 at the second stage in FIG. 5 becomes equal to the probability that the least significant bit becomes "1", which is equal to 1/2.

Accordingly, the distributions as shown in FIGS. 6A and 6B arise at the same probability of "1/2", respectively, and the overall error distribution is as shown in FIG. 6C. Also, the mean square error of this distribution is "0.125".

The values which are the product 1/2 and the inner product between the superposed error and the second, third and fourth row of the transformation matrix in the expression (4), are distributed from "-0.25" to "0.75" at a step of "0.25", in contrast to the distribution of FIG. 6A. Since the value added in the rounding process after the Hadamard transform section at the second stage is symmetrically "-0.5", the overall error distribution is symmetrical, resulting in the same distribution. The input data for other three Hadamard transformations have the same error distribution using the same calculation, though the distribution of superposed error is slightly different, whereby the mean error is "0" and the mean square error is "0.125". Consequently, the mean error becomes "0"

and the mean square error becomes "0.125" in all the outputs y0 to y15 of FIG. 5.

For reference, the configuration not satisfying the above condition (B1) is shown in FIG. 7, and the behavior of the mean error and the mean square error will be described below. The wirings in FIG. 7 are the same as in FIG. 5, but the rounding process is different.

In FIG. 7, since four input data of the Hadamard transform section 521 at the second stage are all the rounded up data, its superposed error is deviated in + direction such as (0, 0, 0, 0) to (+0.5, +0.5, +0.5, +0.5). Therefore, the values which are the product of 1/2 and the inner product between the superposed error and the first row of the transformation matrix in the expression (4), have a distribution as shown in FIG. 8A. Thereafter, if "+0.5" is further added in a rounding process 711, the error distribution is as shown in FIG. 8B, and the overall error distribution is as shown in FIG. 8C. Hence, the mean error of output y0 becomes "0.75", and the mean square error becomes "0.6875". However, the error distribution is the same as in FIG. 6C, with its variance being "0.125". Herein, the mean square error, which is {(mean error)^2 + variance}, becomes larger because the mean error is not "0".

In FIG. 7, the error superposed on any of the outputs y0 to y15 has the same distribution, with its

variance being "0.125". In this way, the mean error is different depending on the output, and the mean square error is varied accordingly. All the outputs are classified into the following three groups, according to the mean error and the mean square error.

Mean error = 0.75, mean square error = 0.6875 : y0

Mean error = 0.25, mean square error = 0.1875 : y7, y8, y15

Mean error = -0.25, mean square error = 0.1875 : others

If the lossless 16-point Hadamard transformation is configured without satisfying the above condition (B1), the errors are superposed as above example.

The lossless 16-point Hadamard transformation according to this embodiment can be easily implemented by the software processing. Each Hadamard transform section of real type can be implemented with the fixed point operation or floating point operation, and the rounding process can be performed in such a way that for rounding up, "0.5" is added and the floor function is acquired, and for rounding down, the floor function is acquired without addition, whereby the equivalent operation for the configuration of FIG. 5 can be made by the software processing.

[Second Embodiment]

In the lossless 16-point Hadamard transformation implemented in the first embodiment, in a case where

the input data is regularly arranged in a 4×4 matrix,
the lossless two-dimensional Hadamard transformation is
realized for the 4×4 two-dimensional data. As a
preparation before showing the configuration for the
two-dimensional process, the mathematical notation is
simplified as shown in the following expression (6).
[Expression 6]

$$
\begin{bmatrix} + & - & - & - \\ - & + & - & - \\ - & - & + & - \\ - & - & - & + \end{bmatrix}
\frac{1}{2}
\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix}
\begin{bmatrix} d0 & d4 & d8 & d12 \\ d1 & d5 & d9 & d13 \\ d2 & d6 & d10 & d14 \\ d3 & d7 & d11 & d15 \end{bmatrix}
\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \\ 1 & -1 & 1 & -1 \end{bmatrix}
\times \frac{1}{2}
\begin{bmatrix} + & - & - & - \\ + & - & + & + \\ + & + & + & - \\ + & + & - & + \end{bmatrix}
\quad (6)
$$

In this expression (6), the first (leftmost) and
the fifth (rightmost) matrices composed of "+" and "-
" signs represent the contents of the rounding process.
Herein, each symbol has the same meaning as "+" and "-
" in FIGS. 4A to 4H. First, the arithmetical operation
is made between the second and third matrices from the
left, the rounding process as defined in the first
matrix is performed after multiplying the factor 1/2.
Then, the arithmetical operation with the fourth matrix
is made, and the rounding process of the last matrix is
made after multiplying the factor 1/2. In the non-
linear arithmetical operation, if the order of
operation is changed, the characteristics are changed.
In this case, unless the rounding operation for the
leftmost matrix is firstly performed, the mean error
becomes non "0".

The transformation in the expression (6) is one
example, and there are 512 types of transformations in
which the mean error becomes "0" as already described.
There is a difference only between the leftmost and
rightmost matrices representing the content of the
rounding process. Hence, the lossless 4×4 two-
dimensional Hadamard transformation (lossless 16-point
Hadamard transformation) are defined by expressing the
two matrices.

On the other hand, the configuration for
implementing this lossless 16-point Hadamard
transformation two-dimensionally is shown in FIG. 9.
Herein, every four data is processed in a vertical
direction, and its results are transposed and processed
in a horizontal direction. The order of processing may
be reversed.

FIG. 9 depicts a block diagram showing the
configuration of the lossless two-dimensional Hadamard
transformation according to the second embodiment of
the invention.

In FIG. 9, numerals 901 and 911 denote Hadamard
transform sections for making the Hadamard
transformation process on the basis of the
transformation matrix of the expression (3) or (4).
Numeral 903 and 913 denote decoders for generating the
addition data to be rounded up in accordance with the
column number and the row number of the two-dimensional

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data to be processed. Numerals 905 and 915 denote

adder sections for making the adding process for

rounding up. Numeral 907 and 917 denote discard

sections for discarding the fraction part, and numeral

5　909 denotes a buffer for temporarily storing the 4×4

two-dimensional data to be transposed (rearranged).

　　　The discard sections 907 and 917 for discarding

the fraction part are provided on the process concept,

but actually implemented by disconnecting the signal

10　line of the fraction part and outputting the integer

part only.

　　　First of all, four data in the first column are

input in parallel into the Hadamard transform section

901. Herein, the transformation process is performed

15　in accordance with the transformation matrix of the

expression (3) or (4). Since the rounding process on

the reverse transformation side is varied by the

transformation matrix, the Walsh type Hadamard

transformation matrix of the expression (4) is employed.

20　The data transformed in this Hadamard transform section

901 is the data having the fraction part of one bit,

and passed to the adder section 905.

　　　On the other hand, the decoder 903 generates the

addition data for rounding up on the basis of the input

25　column number information, and supplies it to the adder

section 905. That is, the addition data (1, 0, 0, 0),

(0, 1, 0, 0), (0, 0, 1, 0) and (0, 0, 0, 1) are

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generated for "1", "2", "3" and "4" that are input as the column number and passed to the adder section 905. These addition data correspond to the column vector of the matrix at the leftmost location in the expression

5   (6), in which "+" and "-" are replaced with "1" and "0", respectively.

The addition data for rounding up is added to the fraction part of the transformed data in the adder section 905. Hence, the weight of the addition data is

10   set to "0.5". And the next discard section 907 discards the fraction part, whereby the rounding process is completed. Herein, when the fraction part of the transformed data is "0", the rounding process performed in the adder section 905 and the discard

15   section 907 has no influence on the transformed data. However, when the fraction part of the transformed data is "1", the transformed data to which "0.5" is added is rounded up, and the other data is discarded.

If the column numbers of four data to be processed

20   are changed, the addition data for rounding up is correspondingly changed, whereby the rounding process for each column number is changed. In this way, the data that has been subjected to the lossless Hadamard transformation is saved in the buffer 909. This buffer

25   909 is so small as to transpose the 4×4 data, and may be easily constructed by a register, for example.

If the lossless transformation process for four columns (column number 4) of data is ended, the data is transposed in the buffer 909 and output as the row data. This row data is subjected to the lossless Hadamard transformation, employing the four-point Hadamard transform section 911, the decoder 913, the adder 915 and the discard section 917. The decoder 913 outputs the addition data corresponding to the row vector in the rightmost matrix of the expression (6). Thereby, the mean error of transformed data after the lossless two-dimensional Hadamard transformation becomes "0", and the mean square error becomes "0.125".

[Modification to the Second Embodiment]

The two adder sections 905 and 915 may be configured to output different data depending on the value of the least significant bit (equal for four data) of the four data output from the corresponding Hadamard transform sections 901 and 911. That is, the adder sections 905 and 915 receives the least significant bit, and outputs the addition data of four "0" when the least significant bit is "0", or outputs "0.5" or "-0.5" when the least significant bit is "1". In other words, the adder sections 904 and 915 receives the least significant bit (L), and outputs (0.5×L) or (-0.5×L). The same process as the rounding process as previously described may be performed for the output from the adder sections 905 and 915.

[Third embodiment]

    This third embodiment is the lossless two-dimensional DCT (Discrete Cosine Transformation), employing the 4×4 lossless two-dimensional Hadamard

5 transformation as described in the second embodiment. The lossless DCT was firstly realized in the following document 1. (Document 1) Kuninori Komatsu and Kaoru Sezaki, "Reversible Discrete Cosine Transformation and its Application to Image Information Compression",

10 Shingaku Giho IE97-83, p.1-6, Nov. 1997.

    In this document 1, it is pointed out that because the Hadamard transformation is not used, a great number of multiplications are performed. As seen from the transformation matrix of the expression (3) or (4), the

15 four-point Hadamard transformation is implemented only by addition and subtraction and the bit shift, and has no need for the multiplication. Though the rounding process is increased with the lossless transformation, it is only necessary to perform the addition to deal

20 with the rounding up process, using the arithmetical operation method according to this invention.

    Also, the lossless DCT using the lossless four-point Hadamard transformation has been offered in the following document 2. The lossless four-point Hadamard

25 transformation as used herein has the configuration of FIG. 2. (Document 2) Shinji Fukuma, Koichi Oyama, Masahiro Iwabashi and Noriaki Kamibayashi, "Lossless 8-

point Fast Discrete Cosine Transformation Applying
Lossless Hadamard Transformation", Shingaku Giho IE99-
65, p.1-6, Dec. 1999.

FIG. 10 depicts a block diagram showing the
configuration of the lossless DCT as described in this
document 2.

In FIG. 10, reference numerals 1001, 1003 and 1005
denote the lossless four-point Hadamard transform
sections, and the two-input and two-output blocks 1006
to 1010 are rotation units for rotating the two-
dimensional vector on the plane. The rotation units
1006 to 1010 are configured as lossless rotation units
with a Ladder Network as described in the document 2.
All the units are made lossless (reversible), whereby
the entire DCT becomes lossless (reversible) to be able
to make the lossless DCT process. This configuration
is only shown with the one-dimensional transformation.

When the two-dimensional DCT is performed, it is
common that the one-dimensional DCT is processed
separately in the horizontal and vertical directions,
as shown in FIG. 11.

FIG. 11 depicts a block diagram showing the
configuration of a conventional lossless two-
dimensional DCT.

In this arithmetical operation order, the lossless
two-dimensional Hadamard transformation is not
performed. Its reason is that a horizontal Hadamard

transformation process 1100 and a vertical Hadamard

transformation process 1101 are separated. Therefore,

it is almost meaningless that the mean error is made

zero. In the arithmetical operation order of the two-

dimensional DCT in FIG. 11, the latter process in the

horizontal direction and the lossless Hadamard

transformation process in the vertical direction may be

exchanged, and performed in the order as shown in FIG.

12, enabling the complete two-dimensional Hadamard

transformation to be made, whereby the new lossless

two-dimensional DCT using the lossless two-dimensional

Hadamard transformation is implemented.

FIG. 12 depicts a diagram showing the

configuration of a lossless two-dimensional DCT

according to a third embodiment of the invention.

FIGS. 11 and 12 show the software process in the

processing order, in which these figures are not in the

flowchart format but closest to the flowchart, and the

corresponding flowcharts are omitted.

Though the configuration as shown in FIG. 10

enables the process to be made in the order as shown in

FIG. 12, it is also possible to make the process with

the configuration as shown in FIG. 13 in the order of

FIG. 12.

FIG. 13 depicts a diagram showing the

configuration of the one dimensional DCT that is

effective for the lossless two-dimensional DCT of FIG.

12. In FIG. 13, the lossless Hadamard transformation
process with two lossless four-point Hadamard transform
sections at the former stage employs the technique as
described in the document 2, while the lossless

transformation process at the latter stage includes a
slight variation of the technique of the document 1.
When the process is performed in the order of FIG. 12,
a configuration of FIG. 13 has a great effect. In
evaluating the transformation precision as will be

described later, the configuration of FIG. 13 is
employed.

The transformation precision of the lossless DCT
is problematical in respect of the compatibility. That
is, the code compressed using the lossless DCT is

decoded by the decoder using the conventional lossy DCT,
there occurs a signal degradation due to miss match of
DCT besides the compression. And this signal
degradation is more predominant for the higher image
quality compression with higher compression ratio.

FIG. 14 depicts a table showing the reverse
transformation precision of the lossless two-
dimensional DCT according to this embodiment. For
reference, the precisions of the lossless two-
dimensional DCTs as described in the documents 1 and 2

are shown for comparison. The precision as shown in
FIG. 14 is calculated on the basis of the specification

of reverse transformation precision for the DCT in the
ITU-T H. 261 standard.

As will be clear from FIG. 14, in the lossless
two-dimensional DCT according to this embodiment, the
5   total pixel mean value of mean square errors and the
maximum value for the pixels are closer as compared
with the methods of the above documents. This means
that there is a less dispersion in the mean square
error between pixels, and all the pixels are degraded
10   almost uniformly. The total pixel mean value of the
mean square errors in this embodiment is decreased to
about "2/3" to "1/2" as compared with the documents 1
and 2, but the maximum value of the mean square error
is decreased to about "1/3" to "1/3.7" as compared with
15   the documents 1 and 2. Moreover, the mean error has
the similar trend. That is, in this embodiment, the
total pixel mean value is doubled or more as compared
with the document 1, but the maximum value is
conversely decreased to about 60%.
20   In this way, with this embodiment, the precision
is improved for all the items, except for the mean
error over all the pixels.

In the embodiments, examples of the two-
dimensional DCT using the two-dimensional Hadamard
25   transformation are described, but upon two-dimensional
Discrete Cosine Transforming 8×8 block data, the 8×8
block data may be segmented into four 4×4 block data

and each 4×4 block data may be two-dimensional transformed using the two-dimensional Hadamard transformation.

This invention may be applied to the system consisting of a plurality of apparatuses (e.g., host computer, interface unit, reader, and printer), or to a single apparatus (e.g., copying machine, and facsimile).

In the embodiments, the Hadamard transformations are implemented using a hardware, but those may be implemented using a software.

Also, the object of the invention is achieved by supplying a storage medium (recording medium) recording a software program code for implementing the functions of the embodiment to the system or apparatus, and reading and executing the program code stored in the storage medium in a computer (or CPU or MPU) of the system or apparatus. In this case, the program code itself read from the storage medium implements the functions of the embodiment, and the storage medium storing the program code constitutes the invention. The functions of the embodiment are implemented when the computer reads and executes the program code. However, the functions of the embodiment may be also implemented when an operating system (OS) of the computer performs a part or all of the process upon an instruction of the program code.

Moreover, the functions of the embodiment may be implemented in such a way that the program code read from the storage medium is written into a function extension card inserted into the computer or a memory

5   equipped for the function extension unit connected to the computer, and the CPU provided for the function extension card or function extension unit performs a part or all of the actual process upon an instruction of the program code.

10   As described above, according to the first embodiment, to construct the lossless 16-point Hadamard transformation, using the 4×2 stage lossless four-point Hadamard transformation, the rounding process at the first stage is configured such that for four

15   intermediate data inputted into the Hadamard transformation at the second stage, the odd number of data is rounded up, and the remaining odd number of data is rounded down, and the rounding process at the second stage is configured such that the Hadamard

20   transformation at the second stage makes the reverse transformation, grasping four input data as coming from the same Hadamard transformation.

Thereby, the mean error of transform coefficients after the lossless transformation can be "0". Also,

25   the lossless two-dimensional Hadamard transformation for 4×4 data in which the mean error of transform coefficients becomes "0" is realized.

Moreover, if the 4×4 lossless two-dimensional
Hadamard transformation is performed in the
arithmetical operation process of the lossless two-
dimensional DCT, the transformation precision of the
5   lossless two-dimensional DCT can be improved over the
conventional method.

Also, in the two-dimensional lossless
transformation device, the rounding process may be
changed depending on the row or column number of the
10   two-dimensional data to be processed, whereby the
transformation precision is improved.

Moreover, if the lossless two-dimensional Hadamard
transformation is performed in the arithmetical
operation process of the lossless two-dimensional DCT,
15   the lossless two-dimensional DCT with high
transformation precision can be realized.

The present invention is not limited to the above
embodiments and various changes and modifications can
be made within the spirit and scope of the present
20   invention. Therefore to apprise the public of the
scope of the present invention, the following claims
are made.